

## Homework #6 Solutions

$$1. S_e = \left[ \frac{2q^2 a_0 Z_1^{1/6} Z_2 N}{\epsilon_0 (Z_1^{2/3} + Z_2^{2/3})^{3/2}} \right] \frac{v}{v_0} \quad (5.14)$$

$$a_0 = 0.53 \times 10^{-8} \text{ cm (Bohr radius)} = 5.3 \times 10^{-11} \text{ m}$$

B

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$v_0 = \text{Bohr velocity} = 2.2 \times 10^6 \text{ m/s}$$

$$Z_1 = 5$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$m_1 = 10.8$$

$$N = 5 \times 10^{22} \text{ cm}^{-3} = 5 \times 10^{28} \text{ m}^{-3}$$

$$\frac{1}{m_H}$$

$$E = \frac{1}{2} m v^2, \text{ so } v = \left( \frac{2E}{m_1} \right)^{1/2}$$

$$Z_2 = 14$$

$$m_H = 1.67 \times 10^{-27} \text{ kg}$$

$$S_e = \left[ \frac{2q^2 a_0 N}{\epsilon_0 v_0} \right] \left( \frac{2}{m_H} \right)^{1/2} E^{1/2} \left[ \frac{Z_1^{1/6} Z_2}{(Z_1^{2/3} + Z_2^{2/3})^{3/2}} \right] \frac{1}{m_1^{1/2}} \quad J = \frac{\text{kg m}^2}{\text{s}^2}$$

$$= 0.24 \left( \frac{E}{m_1} \right)^{1/2} \left[ \frac{Z_1^{1/6} Z_2}{(Z_1^{2/3} + Z_2^{2/3})^{3/2}} \right] \frac{\text{C}^2 \text{ m m}^{-3}}{(\text{V/m})^{1/2} / \text{s} (\text{kg})^{1/2}} \quad J^{1/2} / \text{m}$$

$$= 0.24 (6.25 \times 10^{18} \text{ eV})^{1/2} \frac{1}{100 \text{ cm}} \left( \frac{E}{m_1} \right)^{1/2}$$

$$= 6 \times 10^6 \left( \frac{E}{m_1} \right)^{1/2} \frac{\text{eV}^{1/2}}{\text{cm}} \left[ \frac{Z_1^{1/6} Z_2}{(Z_1^{2/3} + Z_2^{2/3})^{3/2}} \right] = 6.5 \times 10^6 E^{1/2} \frac{\text{eV}^{1/2}}{\text{cm}} \quad (\text{B})$$

$$S_e = -\frac{dE}{dx} \quad dx = -\frac{dE}{S_e} \quad \int_0^{L_{\text{max}}} dx = \int_{30 \text{ keV}}^0 -\frac{dE}{A E^{1/2}} \quad A E^{1/2}$$

$$L_{\text{max}} = -\frac{2 E^{1/2} \text{ cm}}{6.5 \times 10^6 \text{ eV}^{1/2}} \Big|_{30 \text{ keV}}^0 = 5.33 \times 10^5 \text{ cm} = \underline{\underline{0.53 \mu\text{m}}}$$

2. 100keV B

300nm  $TiSi_2$ , 300nm poly

$$R_p = 215.4 \text{ nm}, \Delta R_p = 56.3 \text{ nm}; R_p = 296.8 \text{ nm}, \Delta R_p = 73.5 \text{ nm}$$

$R_p$  scaling:

Scale to  $TiSi_2$ :  $x_{poly}^{eff} = 300 \text{ nm} \left( \frac{215.4}{296.8} \right) = 217.7$

Stack is equivalent to 517.7 nm of  $TiSi_2$

Eg 8.10 Fraction penetrating =  $\frac{1}{2} \text{erfc} \left( \frac{517.7 - 215.4}{\sqrt{2} (56.3)} \right)$   
 $= 3.86 \times 10^{-8}$  ↖ 3.8

Scale to poly (Si):  $x_{TiSi_2}^{eff} = 300 \text{ nm} \left( \frac{296.8}{215.4} \right) = 413.37$

Fraction penetrating =  $\frac{1}{2} \text{erfc} \left( \frac{713.37 - 296.8}{\sqrt{2} (73.5)} \right)$   
 $= 7.1 \times 10^{-9}$  ↖ 4.01

Dose matching:

$$n(x) = \begin{cases} n_{TiSi_2}(x) & 0 < x < 300 \text{ nm} \\ \alpha n_{Si} [x - (413.4 - 300)] & 300 \text{ nm} < x < \infty \end{cases}$$

$$\int_{-\infty}^{\infty} n(x) dx = \frac{1}{2} + \frac{1}{2} \text{erf} \left( \frac{300 - 215.4}{\sqrt{2} (56.3)} \right) + \frac{\alpha}{2} \text{erfc} \left( \frac{413.4 - 296.8}{(73.5) \sqrt{2}} \right) = 1$$

$\underbrace{\hspace{10em}}_{1.06}$ 
 $\underbrace{\hspace{10em}}_{1.21}$

0.933
+  $\alpha (4.35 \times 10^{-2})$ 
= 1

$\alpha = 1.54$

Fraction penetrating =  $\frac{1.54}{2} \text{erfc} \left( \frac{713.4 - 296.8}{\sqrt{2} (73.5)} \right) = 1.1 \times 10^{-8}$  ↖ 4.01

Intermediate value. Differences are due to  $\frac{\Delta R_p}{R_p}$  not being equal.

**8.16. Calculate the change in junction depth for a 40 keV boron threshold adjust implant of  $5 \times 10^{13} \text{ cm}^{-2}$  annealed at  $750^\circ\text{C}$  in a furnace or at  $1000^\circ\text{C}$  in an RTA for a time just long enough to remove all the damage that causes TED. Assume a uniform well doping of  $5 \times 10^{16} \text{ cm}^{-3}$ .**

**Answer:**

The primary formula we will use gives the enhancement in diffusivity while TED lasts

$$Dt_{\text{eff}} = D^* \frac{I}{I^*} \tau_{\text{enh}}$$

For 40 keV boron,

$$R_p \approx 0.14 \mu\text{m} \quad \Delta R_p \approx 0.055 \mu\text{m}$$

The initial junction is given by

$$C_B = \frac{Q_{\text{Si}}}{\sqrt{2\pi\Delta R_p^2}} \exp\left(-\frac{(x - R_p)^2}{2\Delta R_p^2}\right)$$

$$x = 0.3 \mu\text{m}$$

$$D_B = 0.76 \exp\left(-\frac{3.46}{kT}\right)$$

At  $750^\circ\text{C}$ , the equilibrium boron diffusivity is

$$D_B = 6.9 \times 10^{-18} \text{ cm}^2 \text{ sec}^{-1}$$

and it is enhanced by 7500 (Fig. 8.38) for a time of 400 seconds (Fig. 8.40)

giving

$$Dt_{\text{eff}}^{750^\circ\text{C}} = 2.07 \times 10^{-11} \text{ cm}^2$$

At  $1000^\circ\text{C}$ , the equilibrium boron diffusivity is

$$D_B = 1.5 \times 10^{-14} \text{ cm}^2 \text{ sec}^{-1}$$

and it is enhanced by 400 for 0.2 seconds

$$Dt_{\text{eff}}^{1000^\circ\text{C}} = 1.2 \times 10^{-12} \text{ cm}^2$$

Clearly, the effective  $Dt$  is higher at  $750^\circ\text{C}$  than at  $1000^\circ\text{C}$ , and we can calculate the new junction depths from

$$x = R_p + \sqrt{-2(\Delta R_p^2 + 2Dt_{\text{eff}}) \ln \left[ \frac{C_B}{Q} \sqrt{2\pi(\Delta R_p^2 + 2Dt_{\text{eff}})} \right]}$$

$$x = 0.14 + 0.23 = 0.37 \mu\text{m} \text{ at } 750^\circ\text{C}$$

$$x = 0.14 + 0.17 = 0.31 \mu\text{m} \text{ at } 1000^\circ\text{C}$$

The  $1000^\circ\text{C}$  is deeper by

$$\Delta x_j = 0.06 \mu\text{m}$$

$$4 (a) C_{As}(x) = \frac{Q}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x-R_p)^2}{2\sigma^2}\right)$$

$$E_n = 80 \text{ keV} * C_{As}(x)$$

$$C_{\text{damage}} = \frac{E_n(x)}{30 \text{ eV}} = \frac{80,000}{30} \frac{Q}{\sqrt{2\pi} (25 \times 10^{-7} \text{ cm})} \exp\left(-\frac{(x-60)^2}{2(25)^2}\right)$$

Amorphization at peak when  $C_{\text{damage}}(60 \text{ nm}) = 5 \times 10^{21} \text{ cm}^{-3}$  ( $x$  in nm)

$$Q = \frac{5 \times 10^{21} \text{ cm}^{-3} \sqrt{2\pi} (25 \times 10^{-7} \text{ cm}) 30 \text{ eV}}{80,000 \text{ eV}} = \underline{\underline{1.2 \times 10^{13} \text{ cm}^{-2}}}$$

(b) Amorphization at surface when

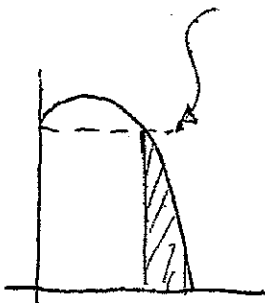
$$C_{\text{damage}}(0) = 5 \times 10^{21} \text{ cm}^{-3}$$

$$Q = 1.2 \times 10^{13} \text{ cm}^{-2} \exp\left(\frac{(60)^2}{2(25)^2}\right) = \underline{\underline{2.1 \times 10^{14} \text{ cm}^{-2}}}$$

(c) Location of a/c interface is when  $C_{\text{damage}}(x) = 5 \times 10^{21} \text{ cm}^{-3}$

$$x_{\text{af}} = 60 \text{ nm} + 25 \text{ nm} * \sqrt{2 \ln\left(\frac{5 \times 10^{21} \text{ cm}^{-3}}{1.7 \times 10^{13} \text{ cm}^{-2} Q}\right)}$$

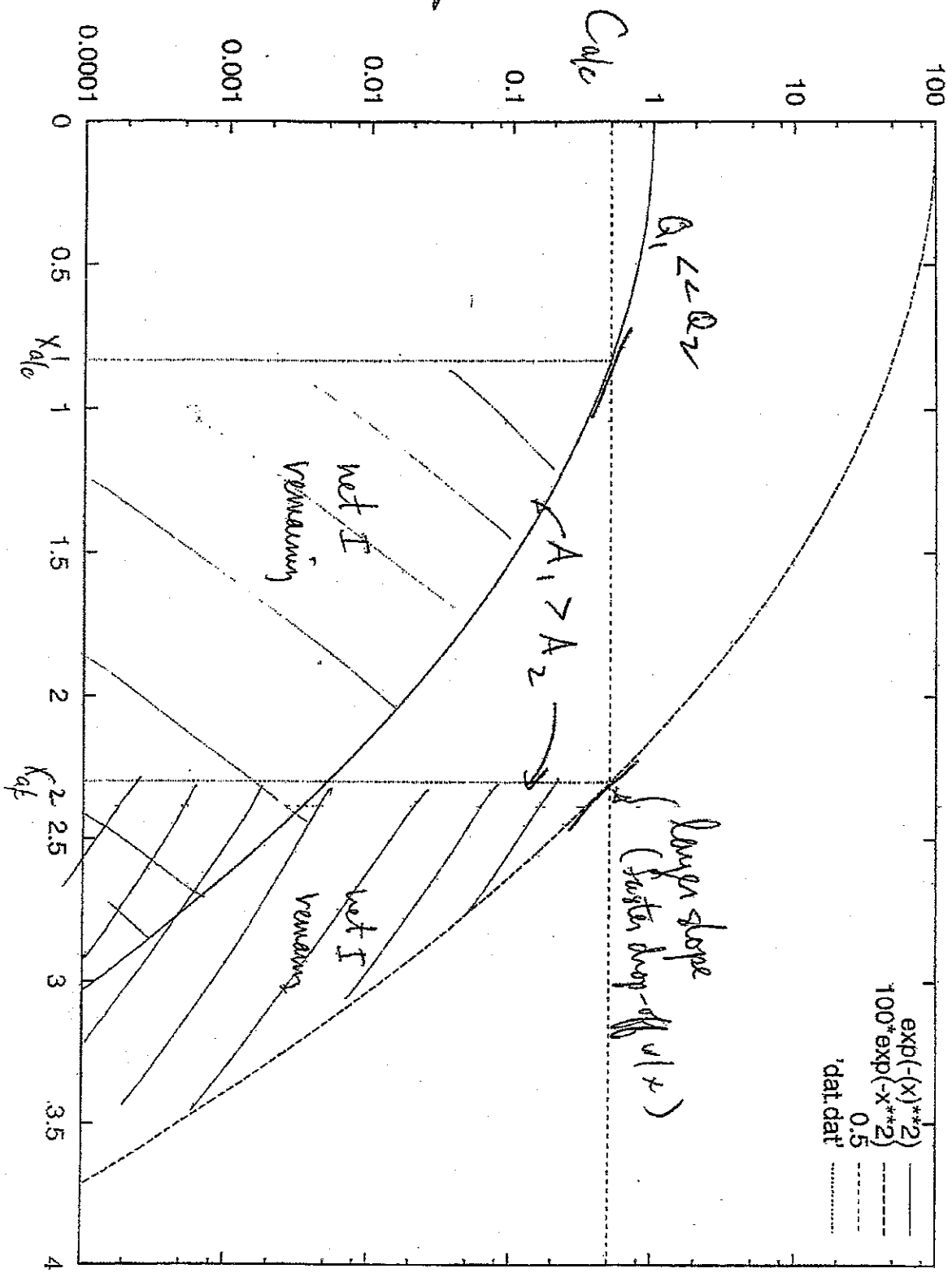
Remaining dose is  $\int_{x_{\text{af}}}^{\infty} C_{\text{damage}}(x) dx$  at  $x_{\text{af}}$   $C_{\text{damage}}$  is the same



$$\begin{aligned} \left. \frac{dC_{\text{damage}}}{dx} \right|_{x=x_{\text{af}}} &= -1.7 \times 10^{13} \text{ cm}^{-1} Q \left( \frac{2(x_{\text{af}}-60)}{2(25)^2} \right) \exp\left(-\frac{(x_{\text{af}}-60)^2}{2(25)^2}\right) \\ &= -\frac{2(x_{\text{af}}-60)}{2(25)^2} 5 \times 10^{21} \text{ cm}^{-3} \end{aligned}$$

This,  $C_{\text{damage}}$  drops faster when  $x_{\text{af}}$  is larger (larger dose)

Total Damage dose decreases w/ implant dose ( $Q$ ) due to increased slope (as shown on plot).



**5.3. An X-ray exposure system uses photons with an energy of 1 keV. If the separation between the mask and wafer is 20  $\mu\text{m}$ , estimate the diffraction limited resolution that is achievable by this system.**

**Answer:**

The equivalent wavelength of 1 keV x-rays is given by

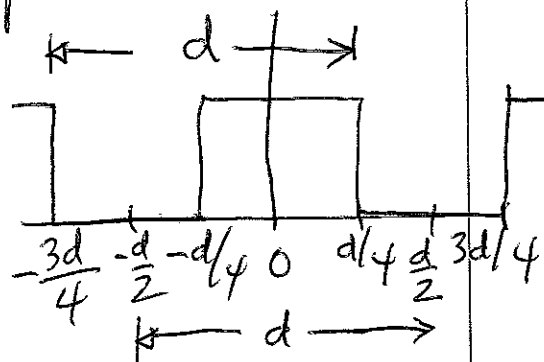
$$E = h\nu = \frac{hc}{\lambda} \quad \therefore \quad \lambda = \frac{hc}{E} = \frac{(4.14 \times 10^{-15} \text{ eV sec})(3 \times 10^{10} \text{ cm sec}^{-1})}{10^3 \text{ eV}}$$
$$= 1.24 \times 10^{-7} \text{ cm} = 1.24 \text{ nm}$$

X-ray systems operate in the proximity printing mode, so that the theoretical resolution is given by Eqn. 5.12:

$$\text{Resolution} = \sqrt{\lambda g} = \sqrt{(1.24 \times 10^{-3} \mu\text{m})(20 \mu\text{m})} = 0.15 \mu\text{m}$$

6. The Fourier decomposition of square wave with unit height and period  $d$  is:

$$\frac{1}{2} + \frac{2}{\pi} \left[ \cos \frac{2\pi x}{d} - \frac{1}{3} \cos \frac{6\pi x}{d} + \frac{1}{5} \cos \frac{10\pi x}{d} - \frac{1}{7} \cos \frac{14\pi x}{d} + \dots \right]$$



Maximum spatial frequency allowed by the pupil function is:

$$\frac{NA}{\lambda} = \frac{0.8}{193 \text{ nm}} = 0.00414 \text{ nm}^{-1}$$

the spatial frequencies are  $\frac{n}{d}$ , where  $n = 1, 3, 5, \dots$

$$\frac{1}{d} = \frac{1}{260 \text{ nm}} = 0.0038, \text{ so only } 1^{\text{st}} \text{ order term}$$

passes through pupil function. The resulting

$$\text{intensity is: } I = I_0 \left[ 0.5 + 0.637 \cos \left( \frac{x}{41.4 \text{ nm}} \right) \right]^2$$

$$\frac{I}{I_0} = \begin{cases} 0.6 @ x = \pm 46.57 \text{ nm} \\ 0.4 @ x = \pm 56.34 \text{ nm} \end{cases}$$

