1. A contact is made between silicon (χ = 4.05eV) doped with Na = 10^{18} \text{cm}^{-3} and aluminum (φ_{ma} = 4.1eV). A high density of surface states pins the Fermi level at 0.4eV above the valence band maxima. Calculate φ_s, φ_B and φ_i (ignoring any narrow tunnelable barrier associated with interface dipole layer) and sketch the band diagram (including vacuum level and with barriers indicated) and the charge density versus position for the contact in equilibrium. (20)
2. If $x_n = 100\text{nm}$, what is the voltage dropped across the depletion region in pn junction with doping shown below (you may assume that width of heavily doped p-type depletion region is negligible)? (15)
3. In an abrupt silicon p-n junction, \( N_a = 5 \times 10^{18}\text{cm}^{-3} \), \( N_d = 2 \times 10^{17}\text{cm}^{-3} \), \( \tau_n = 0.25\mu\text{s} \),
\( \tau_p = 0.16\mu\text{s} \), \( D_n = 4\text{cm}^2/\text{s} \) and \( D_p = 2\text{cm}^2/\text{s} \) in the p-region and \( \tau_n = 0.25\mu\text{s} \), \( \tau_p = 0.16\mu\text{s} \),
\( D_n = 25\text{cm}^2/\text{s} \) and \( D_p = 9\text{cm}^2/\text{s} \) in the n-region, \( W_p = 100\text{nm} \) and \( W_n = 500\mu\text{m} \),
\( T = 300\text{K} \). The applied voltage is 0.7 V. Assume recombination in depletion region can be neglected.

(a) Calculate the hole current density in n-region at edge of depletion region. (10)

(b) Calculate electron current density at contact to p-region contact. (10)

(c) Calculate electron current density at contact to n-region. (10)
4. In a silicon ($\chi_s = 4.15$ V) MOS capacitor with an $n$-type substrate and a heavily p-doped polysilicon gate ($E_f = E_v$), the substrate doping is $N_d = 10^{17}\text{cm}^{-3}$ and the oxide thickness is 5nm. The charge on the gate of $Q_g = -10^{-7}\text{C/cm}^2$.

(a) Determine the state of the channel region (accumulation, flat-band, depletion, strong inversion, etc.). (10)

(b) Sketch the charge density, electric field and energy band diagram for the system. (10)

(c) Determine the applied gate to substrate voltage. (15)